



WSML Deliverable  
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WSML/OWL MAPPING

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# Abstract

This document presents the mapping from WSML-DL to OWL DL, as well as the mapping from OWL DL to WSML-DL. The mapping is applicable to ontologies and logical expressions only, not to Web services, Goals or Mediators. Within this document we currently map the WSML surface syntax (as presented in D16.1, the WSML Language Reference, to OWL and not the WSML abstract syntax (as presented in D16.3, the WSML Abstract Syntax).



# Contents

<b>1</b>	<b>Introduction</b>	<b>4</b>
<b>2</b>	<b>Mapping WSML-DL to OWL DL</b>	<b>5</b>
2.1	Pre-processing Steps . . . . .	5
2.2	Mapping Table . . . . .	6
2.3	Qualified Cardinality Restrictions . . . . .	12
2.3.1	Use owl:someValuesFrom. . . . .	13
2.3.2	Workaround using rdfs:subPropertyOf. . . . .	13
2.3.3	Use a non-endorsed OWL extension. . . . .	13
<b>3</b>	<b>Mapping OWL DL to WSML-DL</b>	<b>14</b>
3.1	Mapping Table . . . . .	14
<b>4</b>	<b>Roundtripping Issues</b>	<b>18</b>
4.1	Mapping Constraints . . . . .	18
4.1.1	Qualified Cardinality Restrictions . . . . .	18
4.1.2	Enumerated Classes . . . . .	18
4.2	Handling Roundtripping . . . . .	18



# 1 Introduction

Within the following chapters we present a WSML/OWL mapping in two directions: from WSML-DL to OWL DL and from OWL DL to WSML-DL. The main purpose of this document is to help people who are common with OWL[2] to understand the relationship of OWL to WSML.

The mapping presented here is applicable to ontologies and logical expressions only, not to Web services, Goals or Mediators. Please note that logical expressions might occur in ontologies, as well as goal and web service capability descriptions. For a mapping of non-ontology constructs except logical expressions the RDF Syntax for WSML has to be used.

This deliverable contains a mapping from WSML-DL to OWL DL. Other WSML variants will not be mapped directly to OWL, since their semantics are not compatible. If a mapping is desired first such an ontology has to be reduced to either WSML-DL or WSML-Core.

Currently this document maps the WSML surface syntax from D16.1[5], WSML Language Reference to OWL abstract syntax [7]. We do not present a mapping from the WSML abstract syntax as presented in D16.3[3], WSML Abstract Syntax and Semantics.



## 2 Mapping WSML-DL to OWL DL

In the following we will provide both the preprocessing steps that we need to do before translating WSML-DL to OWL DL and the actual mapping table.

### 2.1 Pre-processing Steps

In order to simplify the translation from WSML-DL to OWL DL, we try to build simpler expressions. Therefore we perform the following pre-processing steps:

- Replace all compact URIs with full IRIs. For example, “`dc\#title`” is substituted by “`http://purl.org/dc/elements/1.1\#title`”.
- Replace all unnumbered anonymous identifiers by `http://www.wsmo.org/reasoner/anonymous_<system_time_in_milliseconds>-<random_int>`.
- Rewrite all data term shortcuts (“`string`” := `xsd#string("string");` `integer` := `xsd#integer(integer);` `decimal` := `xsd#decimal(decimal)`).
- Replace idlists with single ids (in the case of **ofType**, **impliesType**, **hasValue**, **memberOf** and **subConceptOf**).  
For example, “*Mary*[*hasChild* **hasValue** {*Bob*, *Anna*}]” is replaced by “*Mary*[*hasChild* **hasValue** {*Bob*}]” and “*Mary*[*hasChild* **hasValue** {*Anna*}]”.
- Replace the remaining conceptual syntax, consisting of concepts and instances, by logical expressions. The transformation is done according to [4, Table 8.1].
- Within logical expressions, the following pre-processing steps are applied:
  - Equivalence and right implication is replaced by left implication.  
For example, “*lexpr* **implies** *rexpr*.” is replaced by “*rexpr* **impliedBy** *lexpr*.” and “*lexpr* **equivalent** *rexpr*” is substituted by “*lexpr* **impliedBy** *rexpr* and *rexpr* **impliedBy** *lexpr*.”.
  - Within left implications, left-side conjunctions and right-side disjunctions are eliminated by splitting the expressions. This normalizing step is only applied if the operands of the respective conjunctions or disjunctions do not contain any dependencies from each other.  
For example, the left implication “*A* **and** *B* **impliedBy** *C*” is replaced by “(*A* **impliedBy** *C*) **and** (*B* **impliedBy** *C*)” and the left implication “*A* **impliedBy** *B* **or** *C*” is replaced by “(*A* **impliedBy** *B*) **and** (*A* **impliedBy** *C*)”.
  - If the expression contains unquantified variables, we explicitly universally quantify the variables outside the formula (the WSML language



reference [5, Section 2.8] says: “If a variable is not quantified inside a formula, the variable is implicitly universally quantified outside the formula”). This quantification is applied to all unquantified variables except the root variable. Next we check, step by step, in which molecule inside of the expression a specified variable is contained and push the quantifiers as far as possible inside of the expression.

For example, the expression “**?x memberOf A impliedBy ?x[att1 impliesType ?y] and ?y[att2 impliesType ?z] and ?z memberOf B**” is replaced by “**?x memberOf A impliedBy exists ?y(?x[att1 impliesType ?y] and exists ?z(?y[att2 impliesType ?z] and ?z memberOf B))**”.

## 2.2 Mapping Table

Table 2.1 and Table ?? contain the mapping between the WSML-DL surface syntax and the OWL DL abstract syntax. The mapping is described through the mapping function  $\tau$ . In Table ?? we will introduce the functions  $\varepsilon$  and  $\alpha$ , which are needed for the correct translation of WSML-DL descriptions.

Boldfaced words in the tables refer to keywords in the WSML language. X and Y are meta-variables and are replaced with actual identifiers and variables during the translation, while DES stands for WSML-DL descriptions. IRIs are abbreviated by compact URIs. The prefix ‘wsm1’ stands for ‘http://wsmo.org/wsm1/wsm1-syntax#’, ‘xsd’ stands for ‘http://www.w3.org/2001/XMLSchema#’, ‘owl’ stands for ‘http://www.w3.org/2002/07/owl#’ and ‘wsm12owl’ stands for ‘http://wsm12owlTransformation#’.

WSML-DL	OWL-DL	Remarks
Mapping for ontologies		
$\tau(\text{ontology id } header_1 \dots header_n \text{ ontology\_element}_1 \dots \text{ontology\_element}_n )$	<b>Ontology</b> (id $\tau(header_1)$ ... $\tau(header_n)$ $\tau(\text{ontology\_element}_1)$ ... $\tau(\text{ontology\_element}_n)$ )	A header can contain <i>annotations</i> , <i>usesMediator</i> and <i>importsOntology</i> statements. An <i>ontology\_element</i> can be a <i>concept</i> , an <i>instance</i> or an <i>axiom</i> .
$\tau(\text{annotations id}_1 \text{ hasValue value}_1 \dots \text{id}_n \text{ hasValue value}_n \text{ endAnnotations})$	<b>Annotation</b> (id <sub>1</sub> $\tau(\text{value}_1)$ ) ... <b>Annotation</b> (id <sub>n</sub> $\tau(\text{value}_n)$ )	For annotations on the ontology level “Annotation” instead of “annotation” has to be written.
$\tau(\text{importsOntology id})$	<b>Annotation</b> (owl#import id)	”id” stands for the identifier of a WSML file.
$\tau(\text{usesMediator id})$	<b>Annotation</b> (wsm1#usesMediator id)	As OWL doesn’t have the concept of a mediator, a wsm1#usesMediator annotation is used.



$\tau(\text{datatype\_id}(x_1, \dots, x_n))$	$\tau_{\text{serializer}}(\text{datatype\_id}(x_1, \dots, x_n))^{\wedge\wedge}$ $\tau_{\text{datatypes}}(\text{datatype\_id})$	The function $\tau_{\text{serializer}}$ , which serializes the WSML representation of a data value to a string representation that can be readily used in OWL, is defined in Table 2.3. $\tau_{\text{datatypes}}$ maps eventual WSML datatypes to XML Schema datatypes, according to [5, Table B.1].
$\tau(\text{id})$	id	In WSML an IRI is enclosed by “_” and “”, which are omitted in OWL abstract syntax.
Mapping for axioms		
$\tau(\text{axiom id log\_expr})$	$\tau(\text{log\_expr})$	A log_expr can be a logical expression like the following.
$\tau(\text{id}[\text{att\_id impliesType range\_id}])$	<b>Class</b> (id <b>restriction</b> (att\_id <b>allValuesFrom</b> range\_id) ) <b>ObjectProperty</b> (att\_id)	
$\tau(\text{id}[\text{att\_id ofType range\_id}])$	<b>Class</b> (id <b>restriction</b> (att\_id <b>allValuesFrom</b> range\_id) ) <b>DatatypeProperty</b> (att\_id)	
$\tau(\text{id1 subConceptOf id2})$	<b>Class</b> (id1 <b>partial</b> id2)	
$\tau(\text{id}[\text{att\_id hasValue value}])$	<b>Individual</b> (id <b>value</b> (att\_id $\tau(\text{value}))$ )	
$\tau(\text{id1 memberOf id2})$	<b>Individual</b> (id1 <b>type</b> (id2))	
$\tau(?x[\text{att\_id2 hasValue ?y}]$ <b>impliedBy</b> $?x[\text{att\_id}$ <b>hasValue ?y])</b>	<b>SubProperty</b> (att\_id att\_id2)	A left implication with attribute values as left-hand and right-hand sides is mapped to an OWL subProperty.
$\tau(?x[\text{att\_id hasValue ?y}]$ <b>impliedBy</b> $?x[\text{att\_id hasValue ?z}]$ <b>and</b> $?z[\text{att\_id hasValue ?y}])$	<b>ObjectProperty</b> (att\_id <b>Transitive</b> )	Transitive Property
$\tau(?x[\text{att\_id hasValue ?y}]$ <b>impliedBy</b> $?y[\text{att\_id hasValue ?x}])$	<b>ObjectProperty</b> (att\_id <b>Symmetric</b> )	Symmetric Property
$\tau(?x[\text{att\_id hasValue ?y}]$ <b>impliedBy</b> $?y[\text{att\_id2 hasValue ?x}])$	<b>ObjectProperty</b> (att\_id <b>inverseOf</b> ( att\_id2))	Inverse Property



$\tau(?x \text{ memberOf concept\_id2 impliedBy } ?x \text{ memberOf concept\_id})$	<b>Class</b> (concept_id partial concept_id2)	Equivalence of concepts can be expressed as follows, with A and B being membership molecules: "A equivalent B" := "A impliedBy B and B impliedBy A"
$\tau(?x \text{ memberOf concept\_id impliedBy } ?x[ \text{ att\_id hasValue ?y}])$	<b>ObjectProperty</b> (att_id domain( concept_id ) )	
$\tau(?y \text{ memberOf concept\_id impliedBy } ?x[ \text{ att\_id hasValue ?y}])$	<b>ObjectProperty</b> (att_id range( concept_id ) )	
$\tau(\text{DES1 impliedBy DES2})$	$\alpha(\text{DES1})$ $\alpha(\text{DES2})$ $\text{subClassOf}(\varepsilon(\text{DES2}) \varepsilon(\text{DES1}))$	"A impliedBy B" can be written as "subClassOf(B,A)".
$\tau()$		If $\tau$ is applied for a non-occurring production no translation has to be made.

Table 2.1: Mapping WSML-DL ontologies and axioms to OWL DL

Table 2.2 introduces us to the mapping of WSML-DL descriptions. Those are used inside of axioms, as you can see in Table ???. We need to translate the descriptions to concept expressions and to axioms. Concept expressions are used within other expressions, while the axioms are added as such to the OWL ontology. The mapping  $\tau$  is translated into a tuple of concept expressions and axioms as follows:  $\tau(DES) = (\varepsilon(DES), \alpha(DES))$ .

The table also indicates a mapping for Qualified Cardinality Restrictions (QCRs). In WSML-DL the QCRs are represented by a combination of WSML-DL descriptions. The mapping to OWL DL is done according the workaround with OWL subproperties, described in Section ???.

#### Example of usage of $\varepsilon(DES)$ and $\alpha(DES)$ .

$\alpha$  is used to translate WSML-DL descriptions to axioms that are directly inserted into OWL DL, while  $\varepsilon$  translates the descriptions to concept expressions that are nested into OWL expressions (as e.g. restrictions).

The following very easy example illustrates this:

DES1 impliedBy DES2 is translated to:  
 $\alpha(\text{DES1})$ ,  
 $\alpha(\text{DES2})$ ,  
 $\text{subClassOf}(\varepsilon(\text{DES2}) \varepsilon(\text{DES1}))$

In a concrete example this can look as following:

DES1 =  $?x \text{ memberOf Human}$   
DES2 =  $?x \text{ memberOf Woman}$



Thus we have the following logical expression:  
 $?x \text{ memberOf Human impliedBy } ?x \text{ memberOf Woman}$

$\alpha$  translates to the OWL Class description:

Class(Woman)

Class(Human)

$\varepsilon$  translates to the expressions that are used within the OWL subClassOf expression:

subClassOf(Woman Human)

Instead of Woman we could also have a more complex expression as DES2, as e.g. an intersection of two classes:

DES2 =  $?x \text{ memberOf Woman and } ?x \text{ memberOf Child}$

$\alpha$  for DES2:

Class(Woman)

Class(Child)

$\varepsilon$  for DES2:

intersectionOf(Woman Child)

$\varepsilon$  translates to the whole expression now to:

subClassOf(intersectionOf(Woman Child) Human)

WSML-DL	OWL-DL - concept expression $\varepsilon$	OWL-DL - axiom $\alpha$	Remarks
Mapping for descriptions (DES)			
$\tau(?x \text{ memberOf id})$	id	Class(id)	Description. Membership molecule
$\tau(?x[\text{att\_id hasValue } ?y])$	restriction ( att\_id allValuesFrom( owl:Thing))	ObjectProperty(att\_id)	Description. Attribute value molecule with ?y being an unbound variable withing the outer logical expression.
$\tau(?x[\text{att\_id hasValue } ?y \text{ and } ?y \text{ memberOf id}])$	restriction ( att\_id someValuesFrom( id))	Class(id) ObjectProperty(att\_id)	Description. Attribute value molecule with ?y being a bound variable.
$\tau(\text{DES}_1 \text{ and } \dots \text{ and } \text{DES}_n)$	intersectionOf ( $\varepsilon(\text{DES}_1)$ $\dots, \varepsilon(\text{DES}_n)$ )	$\alpha(\text{DES}_1)$ $\dots$ $\alpha(\text{DES}_n)$	Description. Conjunction
$\tau(\text{DES}_1 \text{ or } \dots \text{ or } \text{DES}_n)$	unionOf( $\varepsilon(\text{DES}_1), \dots, \varepsilon(\text{DES}_n)$ )	$\alpha(\text{DES}_1)$ $\dots$ $\alpha(\text{DES}_n)$	Description. Disjunction



$\tau(\text{neg DES})$	<b>complementOf</b> ( $\varepsilon(\text{DES})$ )	$\alpha(\text{DES})$	Description. Negation
$\tau(\text{exists } ?x ( ?y [ \text{att\_id hasValue } ?x ] \text{ and DES} ))$	<b>restriction</b> ( <b>att\_id someValuesFrom</b> ( $\varepsilon(\text{DES})$ ) )	$\alpha(\text{DES})$ <b>ObjectProperty</b> (att\_id)	Description. Existential quantification
$\tau(\text{exists } ?x ( ?x [ \text{att\_id hasValue } ?y ] \text{ and DES} ))$	<b>restriction</b> ( <b>inverseOf</b> (att\_id) <b>someValuesFrom</b> ( $\varepsilon(\text{DES})$ ) )	$\alpha(\text{DES})$ <b>ObjectProperty</b> (att\_id)	Description. Existential quantification with inverse role.
$\tau(\text{forall } ?x ( \text{DES impliedBy } ?y [ \text{att\_id hasValue } ?x ] ))$	<b>restriction</b> ( <b>att\_id allValuesFrom</b> ( $\varepsilon(\text{DES})$ ) )	$\alpha(\text{DES})$ <b>ObjectProperty</b> (att\_id)	Description. Universal quantification
$\tau(\text{forall } ?x ( \text{DES impliedBy } ?x [ \text{att\_id hasValue } ?y ] ))$	<b>restriction</b> ( <b>inverseOf</b> (att\_id) <b>allValuesFrom</b> ( $\varepsilon(\text{DES})$ ) )	$\alpha(\text{DES})$ <b>ObjectProperty</b> (att\_id)	Description. Universal quantification with inverse role.
$\tau(\text{exists } ?y_1, \dots, ?y_n ( ?x [ \text{att\_id hasValue } ?y_1 ] \text{ and } \dots \text{ and } ?x [ \text{att\_id hasValue } ?y_n ] \text{ and DES and neg}(?y_1 := ?y_2) \text{ and } \dots \text{ and neg}(?y_{n-1} := ?y_n) ))$	<b>restriction</b> ( <b>att\_id ' minCardinality</b> (n) )	$\alpha(\text{DES})$ <b>ObjectProperty</b> (att\_id) <b>ObjectProperty</b> (att\_id ' <b>range</b> ( $\varepsilon(\text{DES})$ ) ) <b>SubPropertyOf</b> (att\_id ' att\_id ) <b>Annotation</b> (wsm12owl: QCR hasValue att\_id)	Description. (Qualified) minCardinality restriction.
$\tau(\text{forall } ?y_1, \dots, ?y_{n+1} ( ?y_1 := ?y_2 \text{ or } \dots \text{ or } ?y_n := ?y_{n+1} \text{ impliedBy } ?x [ \text{att\_id hasValue } ?y_1 ] \text{ and } \dots \text{ and } ?x [ \text{att\_id hasValue } ?y_{n+1} ] \text{ and DES} ))$	<b>restriction</b> ( <b>att\_id ' maxCardinality</b> (n) )	$\alpha(\text{DES})$ <b>ObjectProperty</b> (att\_id) <b>ObjectProperty</b> (att\_id ' <b>range</b> ( $\varepsilon(\text{DES})$ ) ) <b>SubPropertyOf</b> (att\_id ' att\_id ) <b>Annotation</b> (wsm12owl: QCR hasValue att\_id)	Description. (Qualified) maxCardinality restriction.

Table 2.2: Mapping WSML-DL descriptions to OWL DL

Table 2.3 shows the mapping from WSML data values to strings that can be used directly in OWL as lexical representation, followed by a URI reference to the XML Schema[1] datatype, as it's done with RDF typed literals[6] : lexicalFormRIReference. The mapping is defined through the function  $\tau_{serializer}$ .



WSMML data value	String — OWL	Example
Mapping for data values		
$\tau_{serializer}(xsd\#string("any-character*"))$	"any-character*"	<code>xsd#string("Mary Jones")</code> is mapped to <code>"Mary Jones"^^&lt;xsd#string&gt;</code>
$\tau_{serializer}(xsd\#decimal('-?numeric+.numeric+'))$	"-?numeric+.numeric+"	<code>xsd#decimal(-1.5)</code> is mapped to <code>"-1.5"^^&lt;xsd#decimal&gt;</code>
$\tau_{serializer}(xsd\#integer('-?numeric+'))$	"-?numeric+"	<code>xsd#integer(31)</code> is mapped to <code>"31"^^&lt;xsd#integer&gt;</code>
$\tau_{serializer}(xsd\#float('-?numeric+.numeric+?e E'-?numeric+'))$	"-?numeric+.numeric+?e E'-?numeric+"	<code>xsd#float("-60.5e-3")</code> is mapped to <code>"-0.0605"^^&lt;xsd#float&gt;</code>
$\tau_{serializer}(xsd\#double('-?numeric+.numeric+?e E'-?numeric+'))$	"-?numeric+.numeric+?e E'-?numeric+"	<code>xsd#double("58.5E-5")</code> is mapped to <code>"5.85E-4"^^&lt;xsd#double&gt;</code>
$\tau_{serializer}(xsd\#boolean("true-or-false"))$	"true-or-false"	<code>xsd#boolean("true")</code> is mapped to <code>"true"^^&lt;xsd#boolean&gt;</code>
$\tau_{serializer}(xsd\#duration(year, month, day, hour, minute, second))$	"P1Y2M3DT10H30M20S"	<code>xsd#duration(1, 2, 3, 5, 20, 10)</code> is mapped to <code>"P1Y2M3DT5H20M10S"^^&lt;xsd#duration&gt;</code>
$\tau_{serializer}(xsd\#dateTime(year, month, day, hour, minute, second, timezone-hour, timezone-minute))$	"year-month-dayThour:minute:second-timezone-hour:timezone-minute"	<code>xsd#dateTime(1977, 02, 07, 5, 20, 10, 12, 30)</code> is mapped to <code>"1977-02-07T5:20:10-12:30"^^&lt;xsd#dateTime&gt;</code>
$\tau_{serializer}(xsd\#dateTime(year, month, day, hour, minute, second))$	"year-month-dayThour:minute:second"	<code>xsd#dateTime(1977, 02, 07, 5, 20, 10)</code> is mapped to <code>"1977-02-07T5:20:10"^^&lt;xsd#dateTime&gt;</code>
$\tau_{serializer}(xsd\#time(hour, minute, second, timezone-hour, timezone-minute))$	"hour:minute:second-timezone-hour:timezone-minute"	<code>xsd#time(5, 20, 10, 12, 30)</code> is mapped to <code>"5:20:10-12:30"^^&lt;xsd#time&gt;</code>
$\tau_{serializer}(xsd\#time(hour, minute, second))$	"hour:minute:second"	<code>xsd#time(5, 20, 10)</code> is mapped to <code>"5:20:10"^^&lt;xsd#time&gt;</code>
$\tau_{serializer}(xsd\#date(year, month, day, timezone-hour, timezone-minute))$	"year-month-day-timezone-hour:timezone-minute"	<code>xsd#date(1967, 08, 16, 12, 30)</code> is mapped to <code>"1967-08-16-12:30"^^&lt;xsd#date&gt;</code>
$\tau_{serializer}(xsd\#date(year, month, day))$	"year-month-day"	<code>xsd#date(1967, 08, 16)</code> is mapped to <code>"1967-08-16"^^&lt;xsd#date&gt;</code>



$\tau_{serializer}(xsd\#gyearmonth(\text{year}, \text{month}))$	“ year – month ”	xsd#gyearmonth(1977, 02) is mapped to “1977-02” ^^<xsd#gyearmonth>
$\tau_{serializer}(xsd\#gyear(\text{year}))$	“ year ”	xsd#gyear(1977) is mapped to “1977” ^^<xsd#gyear>
$\tau_{serializer}(xsd\#gmonthday(\text{month}, \text{day}))$	“ month – day ”	xsd#gmonthday(12, 06) is mapped to “12-06” ^^<xsd#gmonthday>
$\tau_{serializer}(xsd\#gday(\text{day}))$	“ day ”	xsd#gday(24) is mapped to “24” ^^<xsd#gday>
$\tau_{serializer}(xsd\#gmonth(\text{month}))$	“ month ”	xsd#gmonth(10) is mapped to “10” ^^<xsd#gmonth>
$\tau_{serializer}(xsd\#hexbinary(\text{hexadecimal-encoding}))$	“ hexadecimal – encoding ”	xsd#hexbinary(“0FB7”) is mapped to “0FB7” ^^<xsd#hexbinary>
$\tau_{serializer}(xsd\#base64binary(\text{hexadecimal-encoding}))$	“ hexadecimal – encoding ”	xsd#base64binary(“R01G0DdhNgAPAATyP”) is mapped to “R01G0DdhNgAPAATyP” ^^<xsd#base64binary>

Table 2.3: Mapping WSML data values to strings

## 2.3 Qualified Cardinality Restrictions

Cardinality restrictions are used to constrain the number of values of a particular property, irrespective of the value type. If we also want to specify the values to be of a particular type, we need “qualified cardinality restrictions” (QCR).

One famous example for QCRs in the human anatomy use case is mentioned by Alain Rector in [8]: “The normal hand has exactly five fingers of which one is a thumb”. The fact that a hand has exactly five fingers is easy to describe via a simple cardinality constraint:

```
Class(NormalHand
  restriction (hasFinger cardinality (5)))
```

But without QCRs we cannot describe that one of these fingers must be a thumb.

The Web Ontology Working Group has postponed the issue of full representation of QCRs, but has already proposed an OWL representation for them [10] and discussed a possible workaround that Alain Rector described in [8].

A W3C working draft [9] discusses a partial work-around within the OWL standard and a non endorsed extension of OWL, that allows to express QCRs correctly.



### 2.3.1 Use owl:someValuesFrom.

The construct `owl:someValuesFrom` is equivalent to a QCR with a minimum cardinality of 1. This means that the specified property should have at least one value of this type.

E.g., an Italian dinner should contain at least one antipasto:

```
Class( ItalianDinner partial
  restriction (hasCourse someValuesFrom(AntiPasto)))
```

### 2.3.2 Workaround using rdfs:subPropertyOf.

The idea of the workaround is to express QCRs by having extra subproperties for each component whose number is to be specified. So we introduce a `subPropertyOf` for the main property and then introduce an unqualified cardinality restriction on that `subProperty`.

Using this workaround, the "normal hand" example from human anatomy use case, mentioned before, would be represented by:

```
Class( Finger )
Class( Thumb partial Finger )
ObjectProperty( hasFinger range( Finger ) )
ObjectProperty( hasThumb range( Thumb ) )
SubPropertyOf( hasThumb hasFinger )
Class( NormalHand partial
  restriction ( hasFinger cardinality( 5 ) )
  restriction ( hasThumb cardinality( 1 ) ) )
```

Unfortunately this workaround is not complete (see [9]) and, although it may be ok for simple cases, it can lead to vast and cumbersome numbers of subproperties.

This workaround using the RDFS `subPropertyOf` statement is the one that we use for mapping WSML-DL to OWL DL in Section ??.

### 2.3.3 Use a non-endorsed OWL extension.

Qualified Restrictions resemble regular restrictions but contain one extra triple in the RDF representation and an extra argument in the abstract syntax. This statement would be `valuesFrom`, which points to the value type being restricted.

Using this extension, the normal hand example can be described by:

```
Class( NormalHand partial
  restriction ( hasFinger cardinality( 5 ) )
  qualifiedRestriction ( hasFinger valuesFrom ( Thumb ) cardinality( 1 ) ) )
```

This representation is legal in OWL Full, but the semantics will only be treated correctly by parsers and classifiers that support QCRs.



## 3 Mapping OWL DL to WSML-DL

In the following we will provide the mapping table that allows us to translate OWL DL to WSML-DL.

OWL DL descriptions can mostly be used in a nested way. In the following we will call these descriptions “*ELEMENTs*”. An *ELEMENT* will either be of type class or an anonymous class, i.e., a property restriction, an intersection, a union or a complement description. The translation to WSML works in an analogous way: an *ELEMENT* can be either a concept or a WSML-DL description that can be used in a nested way.

### 3.1 Mapping Table

Table 3.1 contains the mapping between the OWL DL abstract syntax and the WSML-DL surface syntax. The mapping is described through the mapping function  $\tau$ .

Boldfaced words in the table refer to keywords in the WSML language. X and Y are meta-variables that are created in WSML from actual identifiers during the translation. IRIs are abbreviated by compact URIs. The prefix ‘wsm1’ stands for ‘<http://wsmo.org/wsm1/wsm1-syntax#>’, ‘owl’ stands for ‘<http://www.w3.org/2002/07/owl#>’, ‘xsd’ stands for ‘<http://www.w3.org/2001/XMLSchema#>’ and ‘owl2wsm1’ stands for ‘<http://owl2wsm1Transformation#>’.

OWL-DL	WSML-DL	Remarks
Namespace		
Namespace (id = nid)	<b>namespace</b> id _"nid"	
Ontology Header		
<b>Ontology</b> (oid)	<b>ontology</b> _"oid"	
<b>Annotation</b> (annotID text )	<b>annotations</b> annotID <b>hasValue</b> "text " <b>endAnnotations</b>	
<b>Annotation</b> (owl:imports oid)	<b>importsOntology</b> _"oid " <b>annotations</b> owl2wsm1#import <b>hasValue</b> oid <b>endAnnotations</b>	In OWL RDF/XML syntax the import statement looks like the following: <owl:imports rdf:resource="oid" \>.
<b>Annotation</b> (owl2wsm1#import oid)	<b>importsOntology</b> _"oid "	If an ontology was imported initially in a wsm1 file. See Section 4.2 for details.



Classes		
<b>Class</b> (id <b>partial</b> )	<b>concept</b> id	
<b>Class</b> (id <b>partial</b> Element <sub>1</sub> ... Element <sub>n</sub> )	<b>concept</b> id <b>subConceptOf</b> {Element <sub>1</sub> ... Element <sub>n</sub> }	
<b>Class</b> (id <b>complete</b> Element <sub>1</sub> ... Element <sub>n</sub> )	?x <b>memberOf</b> id <b>equivalent</b> Element <sub>1</sub> <b>equivalent</b> ... <b>equivalent</b> Element <sub>n</sub>	equivalence - complete statement
<b>DisjointClasses</b> (id <sub>1</sub> ... id <sub>n</sub> )	?x <b>memberOf</b> id <sub>1</sub> <b>implies</b> neg(?x <b>memberOf</b> id <sub>2</sub> ) <b>and</b> ... <b>and</b> neg(?x <b>memberOf</b> id <sub>n</sub> )	disjoint statement
PropertyRestriction		
<b>restriction</b> (prop_id <b>allValuesFrom</b> (id1)) <b>ObjectProperty</b> (prop_id range(id2))	<b>concept</b> id1 prop_id <b>impliesType</b> id2 <b>annotations</b> annotID <b>hasValue</b> owl2wsm#simpleClass <b>endAnnotations</b>	allValuesFrom
<b>restriction</b> (prop_id <b>allValuesFrom</b> (ELEMENT))	<b>forall</b> ?x(?y[ prop_id <b>hasValue</b> ?x] <b>impliesType</b> ELEMENT)	allValuesFrom
<b>restriction</b> (prop_id <b>someValuesFrom</b> (ELEMENT))	<b>exists</b> ?x(?y[ prop_id <b>hasValue</b> ?x] <b>and</b> ELEMENT)	someValuesFrom - minimal cardinality of 1
<b>restriction</b> (prop_id <b>value</b> (ELEMENT))	?x[ prop_id <b>hasValue</b> ELEMENT]	value
<b>restriction</b> (prop_id <b>minCardinality</b> (n)) <b>ObjectProperty</b> (prop_id range(id))	<b>exists</b> ?x <sub>1</sub> , ..., ?x <sub>n</sub> (?x[ prop_id <b>hasValue</b> ?x <sub>1</sub> ] <b>and</b> ... <b>and</b> ?x[ prop_id <b>hasValue</b> ?x <sub>n</sub> ] <b>and</b> ?x <sub>1</sub> <b>memberOf</b> id <b>and</b> ... <b>and</b> ?x <sub>n</sub> <b>memberOf</b> id <b>and</b> neg(?x <sub>1</sub> = ?x <sub>2</sub> ) <b>and</b> ... <b>and</b> neg(?x <sub>n-1</sub> = ?x <sub>n</sub> ))	minCardinality
<b>restriction</b> (prop_id <b>maxCardinality</b> (n)) <b>ObjectProperty</b> (prop_id range(id))	<b>forall</b> ?x <sub>1</sub> , ..., ?x <sub>n</sub> (?x[ prop_id <b>hasValue</b> ?x <sub>1</sub> ] <b>and</b> ... <b>and</b> ?x[ prop_id <b>hasValue</b> ?x <sub>n</sub> ] <b>implies</b> (?x <sub>1</sub> = ?x <sub>2</sub> ) <b>) or</b> ... <b>or</b> (?x <sub>n-1</sub> = ?x <sub>n</sub> ) <b>) and</b> ?x <sub>1</sub> <b>memberOf</b> id <b>and</b> ... <b>and</b> ?x <sub>n</sub> <b>memberOf</b> id)	maxCardinality



<b>restriction</b> (prop_id cardinality (n) ) <b>ObjectProperty</b> (prop_id range(id))	<b>exists</b> $?x_1, \dots, ?x_n$ ( $?x[\text{prop\_id}$ <b>hasValue</b> $?x_1]$ <b>and</b> ... <b>and</b> $?x[\text{prop\_id}$ <b>hasValue</b> $?x_n]$ <b>and</b> $?x_1$ <b>memberOf</b> id <b>and</b> ... <b>and</b> $?x_n$ <b>memberOf</b> id <b>and</b> <b>neg</b> ( $?x_1 = ?x_2$ ) <b>and</b> ... <b>and</b> <b>neg</b> ( $?x_{n-1} = ?x_n$ ) <b>and</b> <b>forall</b> $?x_1, \dots, ?x_n$ ( $?x$ $[\text{prop\_id}$ <b>hasValue</b> $?x_1]$ <b>and</b> ... <b>and</b> $?x[\text{prop\_id}$ <b>hasValue</b> $?x_n]$ <b>implies</b> ( $?x_1 = ?x_2$ ) <b>or</b> ... <b>or</b> ( $?x_n$ $-1 = ?x_n$ ) <b>and</b> $?x_1$ <b>memberOf</b> id <b>and</b> ... <b>and</b> $?x_n$ <b>memberOf</b> id)	cardinality
<b>intersectionOf</b> (ELEMENT <sub>1</sub> ... ELEMENT <sub>n</sub> )	ELEMENT <sub>1</sub> <b>and</b> ... <b>and</b> ELEMENT <sub>n</sub>	intersection
<b>unionOf</b> (ELEMENT <sub>1</sub> ... ELEMENT <sub>n</sub> )	ELEMENT <sub>1</sub> <b>or</b> ... <b>or</b> ELEMENT <sub>n</sub>	union
<b>complementOf</b> (ELEMENT)	<b>neg</b> (ELEMENT)	complement
Properties		
<b>ObjectProperty</b> (prop_id domain(id1) range(id2))	<b>concept</b> id1 prop_id <b>impliesType</b> id2	ObjectProperty
<b>DatatypeProperty</b> (prop_id domain(id) range(xsd:Datatype))	<b>concept</b> id prop_id <b>ofType</b> xsd#Datatype	DatatypeProperty. We do not explain the mapping of datatypes in detail as this mapping is straightforward: both WSML and OWL use XML Schema[1] Datatypes.
<b>ObjectProperty</b> (prop_id1 super( prop_id2) domain(id1) range( id2))	<b>concept</b> id1 prop_id1 <b>impliesType</b> id2  <b>axiom</b> <b>definedBy</b> $?x[\text{prop\_id2}$ <b>hasValue</b> $?y]$ <b>impliedBy</b> $?x[\text{prop\_id1}$ <b>hasValue</b> $?y]$ .	ObjectProperty with super property
<b>SubPropertyOf</b> (prop_id1 prop_id2)	$?x[\text{prop\_id2}$ <b>hasValue</b> $?y]$ <b>impliedBy</b> $?x[\text{prop\_id1}$ <b>hasValue</b> $?y]$ .	subproperty statement
<b>ObjectProperty</b> (prop_id <b>Transitive</b> domain(id1) range(id2))	$?x[\text{prop\_id}$ <b>hasValue</b> $?z]$ <b>impliedBy</b> $?x[\text{prop\_id}$ <b>hasValue</b> $?y]$ <b>and</b> $?y[\text{prop\_id}$ <b>hasValue</b> $?z]$ .	transitive statement
<b>ObjectProperty</b> (prop_id <b>Symmetric</b> domain(id1) range(id2))	$?x[\text{prop\_id}$ <b>hasValue</b> $?y]$ <b>impliedBy</b> $?y[\text{prop\_id}$ <b>hasValue</b> $?x]$ .	symmetric statement



<b>ObjectProperty(prop_id Functional)</b>	<b>forall</b> $?x, ?y, ?z(?x[prop\_id \text{ hasValue } ?y] \text{ and } ?x[prop\_id \text{ hasValue } ?z] \text{ implies } (?y = ?z) \text{ and ELEMENT})$ .	functional statement - maxCardinality = 1
<b>ObjectProperty(prop_id1 inverseOf(prop_id2))</b>	$?x[prop\_id1 \text{ hasValue } ?y] \text{ impliedBy } ?y[prop\_id2 \text{ hasValue } ?x]$ .	inverse statement
<b>ObjectProperty(prop_id1 InverseFunctional)</b>	<b>forall</b> $?x, ?y, ?z(?y[prop\_id \text{ hasValue } ?x] \text{ and } ?z[prop\_id \text{ hasValue } ?x] \text{ implies } (?y = ?z) \text{ and ELEMENT})$ .	inverse functional statement
<b>EquivalentProperties(prop_id1 ... prop_id_n)</b>	$?x[prop\_id_1 \text{ hasValue } ?y] \text{ equivalent } \dots \text{ equivalent } ?x[prop\_id_n \text{ hasValue } ?y]$ .	equivalent property statement
<b>Individuals</b>		
<b>Individual(id)</b>	<b>instance</b> id	
<b>Individual(id type(class_id))</b>	<b>instance</b> id <b>memberOf</b> class_id	
<b>Individual(id type(class_id) value(prop_id_1 value) ... (prop_id_n value))</b>	<b>instance</b> id <b>memberOf</b> class_id prop_id_1 <b>hasValue</b> value ... prop_id_n <b>hasValue</b> value	
<b>SameIndividual(id_1 ... id_n)</b>	id_1 = id_2 <b>and</b> ... <b>and</b> id_1 = id_n.	same individual
<b>DifferentIndividuals(id_1 ... id_n)</b>	id_1 = <b>neg</b> (id_2) <b>and</b> ... <b>and</b> id_1 = <b>neg</b> (id_n).	different individuals
<b>Enumerated Classes</b>		
<b>EnumeratedClass(class_id ind_1 ... ind_n)</b>	<b>annotations</b> owl2wsm1#enumeratedClass/ class_id/1 <b>hasValue</b> ind_1 ... owl2wsm1#enumeratedClass/ class_id/n <b>hasValue</b> ind_n <b>endAnnotations</b>	enumerated classes do not exist in WSML - we mark in an annotation to the ontology that we removed these from the resulting WSML ontology

Table 3.1: Mapping OWL-DL ontologies to WSML-DL



## 4 Roundtripping Issues

In the following we will first outline some problems that appear while trying to translate WSML-DL to OWL DL and the other way around.

### 4.1 Mapping Constraints

The mappings (from WSML-DL to OWL DL and the other way around) that we presented in 2 and Chapter 3 is not complete. This is due to the fact that both WSML-DL and OWL DL are based on different Description Logic dialects: WSML-DL is based on *SHIQ(D)*, while OWL DL is based on *SHOIN(D)*. [11] explains in more detail the similarities and differences between these two dialects.

#### 4.1.1 Qualified Cardinality Restrictions

Whereas qualified cardinality restrictions can be expressed in WSML-DL, they cannot be expressed in OWL DL. There exist nevertheless some possible workarounds for this in OWL. For a more elaborated discussion on these, see Section 2.3. We have mapped the qualified cardinality restrictions from WSML-DL to OWL DL using the workaround with the `subPropertyOf` statements, although this is, as described in 2.3 not complete.

#### 4.1.2 Enumerated Classes

WSML-DL does not support enumerated classes, as does OWL DL. This allows one to write enumerations of individuals in OWL using the `oneOf` statement:

```
oneOf(Monday, Tuesday, Wednesday, Thursday, Friday, Saturday, Sunday)
```

### 4.2 Handling Roundtripping

We have introduced two namespaces that allows us to make annotations in the ontology that is being newly created, be it a WSML or an OWL ontology:

- `http://owl2wsmlTransformation`
- `http://wsml2owlTransformation`

We use these namespaces in the mapping to indicate cases where we cannot translate ontology elements in a straightforward way, as e.g. due to the mapping constraints mentioned before in Section 4.1.



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